

MA 670-1C – TOPOLOGY I
SPRING 2025

Class meets: Monday, Wednesday, Friday 10:10–11:00, UH 4002

Instructor: Dr. Nándor Simányi

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Office hours: Mondays and Wednesdays, 12:00–1:00.

Special web site dedicated to this course:

<https://people.cas.uab.edu/~simanyi/teaching/MA-670-2025/>

Textbook.

James R. Munkres: Topology, 2nd Edition. Prentice Hall, 2000. (A copy of this book can be found on the website dedicated to this class.)

We will cover Chapters 2 and parts of Chapter 3 of the textbook. This includes the following topics:

1. Basics:

Topology: definition, basis, subbasis. Fundamental examples: order, $X \times Y$, subspace. Closure: closed sets, limit points, Hausdorff spaces. Continuity: equivalent definitions, constructing, homeomorphisms and embeddings.

Product topology: basis and subbasis, box and product topologies compared: R^n , R^ω .

Metric spaces: basics, comparison of metrics, uniform topology, sequence lemma, uniform limits.

2. Connectedness:

Connected spaces and sets: definition, continuity. Products: finite, arbitrary, R^n , R^ω .

Ordered spaces: linear continua, real line, first uncountable ordinal. Components and path components: $\sin(1/x)$ continuum. Local connectedness: $\sin(1/x)$ continuum, R^n .

3. Compactness:

Compact spaces: definition, finite products, finite intersection condition. Ordered spaces: greatest lower bound and least upper bound, real line, first uncountable ordinal. Limit point and sequential compactness: equivalence in metric spaces. Local compactness: one point compactification; $[0, \infty]$ and $[\infty, \infty]$. Totally bounded and compact metric spaces; the Arzela-Ascoli Theorem.

Class Attendance: Class attendance is mandatory. One can get a passing grade only if the number of their unexcused absences is not more than 20% of the number of classes.

Grading.

The course grade will comprise the following:

Regular weekly homework: 30%

Two midterm tests: 15% each

Final exam: 40%

Important Note. Please make sure that you are able to receive e-mail through your Blazer-ID account. Official course announcements will be sent to that address.