$MA\ 411$ - $7P-Integrating\ Mathematical\ Ideas$

UAB Department of Mathematics - Spring 2025

Instructor: Dr. Tricia Phillips

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Class Time: W 5-7:30pm (University Hall 4002)

Office Hours: M 2:30-3:30, W 3:30-4:30, R 9:30-10:30, or by appointment

Office: University Hall 4053

Phone: 205-934-2154

Class Materials: Required: graph paper and a binder or folder for organization; Optional: scissors, ruler, colored pencils/pens or highlighters. There is no official textbook for this course.

Course Description: (3 semester hours). This course will integrate ideas from algebra, geometry, probability, and statistics. Emphasis will be on using functions as mathematical models, becoming fluent with multiple representations of functions, and choosing the most appropriate representations for solving a specific problem. Students will be expected to communicate mathematics verbally and in writing through small group, whole group, and individual interactions. *Prerequisite*: Min grade of C in (MA 125 or MA 225) and MA 314, or MA 316, or MA 168.

Course Overview:

This course serves as the capstone course for the Mathematical Reasoning Track. It will help students achieve an integrated working grasp of mathematical ideas, engage students in inquiry and reflection in the learning and practice of mathematics, help students develop a productive disposition in tackling mathematical problems, and develop the ability to communicate mathematics and mathematical ideas at all levels, both verbally and in writing.

The course will continue the inquiry-based learning environment of other courses in the Mathematical Reasoning Track. The course will integrate ideas from numbers, algebra, geometry, probability, and statistics. In doing this the student will gain understanding and ability in plausible reasoning, conjecture, and justification in the study of patterns and models, functions, and use of technology. The course will emphasize the use of functions as mathematical models, the various ways of representing functions, and the power and uses of these representations in different contexts. Inquiry-based learning will pervade the course, as well as an emphasis on communication skills.

Learning Outcomes: Upon successful completion of this course, a student will be able to:

- apply reasoning to problems, including:
 - deductive reasoning
 - mathematically convincing arguments (leading to mathematical proofs)
 - inductive reasoning
 - reasoning by analogy
 - plausible reasoning
 - educated guessing
 - critical ability
- identify patterns in data, geometry, pictures, algebra, probability, and numbers, and develop models, including:

- using conjecturing and plausible reasoning in finding significant patterns
- functional relations based on patterns
- building algebraic models from geometric and numerical patterns
- exact and approximate representations
- demonstrate knowledge of relations and functions, including:
 - concept of a function and notions of dependence, dependent and independent variables, domain and range
 - multiple ways to represent a function, the questions they help us answer, advantages and disadvantages of each, and transforming one type of representation into another, with representations including:
 - * verbal descriptions of functions
 - * graphical representations
 - * numerical/tabular data
 - * algebraic representations (mathematical formulas):
 - · functional notation and its uses
 - · discrete and continuous variables
 - · continuous and discontinuous functions
 - · piecewise-defined functions
 - · comparison of functions
 - \cdot slope and rate of change
 - · transformations and combinations of functions
 - * special types of functions, with practical, everyday examples of each:
 - · linear functions, slope and intercept (extensive and varied approaches to these, with many examples of sources)
 - · piecewise linear functions
 - · quadratic functions
 - · higher order polynomial functions
 - · rational functions
 - · exponential and logarithmic functions
 - · trigonometric functions and periodic or repetitive phenomena or behavior
 - \cdot functions not fitting into any standard mathematical category, and how to deal with them
- communicate mathematical ideas orally and in writing including making mathematically convincing arguments;
 - mathematics is not just a collection of techniques but is a structured body of knowledge essential to the modern community and to science
 - writing is essential to mathematics: in proofs, explanations, descriptions, and in communication to others (e.g., teaching) and to ourselves
 - understanding that "if you can't explain it, you don't fully understand it"
- demonstrate the ability to interact within groups, and with the class as a whole, while demonstrating cognizance of working with peers at different levels; and
- demonstrate a positive disposition toward persistence and reflection in doing mathematics.

Grades

Grade Components: All grades will be posted on Canvas.

Assignment	Percent
Attendance/Participation	4
Reading Reflections	6
Menus	25
Project	5
Midterm Exam	25
Mathematics Portfolio	10
Final Exam	25

Final Grades: The final grade for this course will be assigned using the following scale:

Total Points	90-100	80-89	70-79	60-69	0-60
Letter Grade	A	В	С	D	F

Specific grade cases:

- Earning an overall A on coursework prior to the Final Exam *and* having perfect attendance throughout the term will make the Final Exam optional.
- Missing 4 or more classes during the semester that are unexcused will result in an automatic F for the course.

Assignment Descriptions

Attendance/Participation:

Attendance and active participation in all class sessions is required. Attending class but not actively participating results in a score of 50% for that class session. Attending class and actively participating results in a score of 100% for that class session.

Reading Reflections:

You will submit a 1 - 1.5 page reflection on Canvas by the beginning of class on the due date for each reading assigned either in paragraph or bullet form. Participation in class discussions regarding the readings are also required.

Menus:

Menus consist of a set of problems you will work on solving throughout the term and that which you will hand in a neatly written / scanned PDF on Canvas by the beginning of class on the given due dates. Using GoodNotes is a great option if you choose to write on a tablet and submit the PDF.

Project:

This assignment will offer students the opportunity to create a visual, aural, or tactile representation of the concepts and tasks we have covered in class. You will submit your project on Canvas by the beginning of class on the given due date.

Midterm Exam:

This will occur during our regularly scheduled class time and a set of problems will be given to solve.

Mathematics Portfolio:

This assignment will include tasks to demonstrate the development and growth of your conceptual understanding, use of processes and strategies, problem-solving abilities, and abilities to communicate mathematically. You will submit a PDF on Canvas by the beginning of class on the given due date.

Final Exam:

This will be a take-home final in which a set of problems will be given to solve. You will submit a PDF on Canvas on the due date. *Note*: If you achieve an A in the course prior to the Final Exam and have perfect attendance, you are not required to take the Final Exam.

Note: For MA 511 students, there will be an additional set of more challenging problems on one or more of the exams so they can demonstrate a higher level of understanding.

Class Policies & Student Expectations

Class Preparation & Collaboration:

I expect you to show respect to the instructor and classmates by putting away distracting items such as cell phones and coursework not related to our class. I ask that you have a positive and productive disposition toward yourself, your classmates, and mathematics and are respectful of fellow classmates and the instructor as you share ideas. During group work, I expect everyone to contribute to the discussion (if you don't know how to answer the question, then ask a question).

You are expected to spend a substantial amount of time working through the course activities and assignments every week. Please know that time management and self-motivation are key components for success in this course. In addition to class time, you should spend about 6 hours per week reading, studying, preparing for class discussions, and/or completing assignments.

You may collaborate with peers on solving menu tasks. However, it is imperative that you are able to solve problems on your own to be prepared for the exams. A good guideline is that after you have solved a problem, you should feel confident that you are able to explain your solution to the class.

Make-up Policy:

Late Work: There are no make-ups for assignments and no late submissions are accepted – all deadlines are in Central Time. It is recommended that students work far in advance of deadlines to ensure they finish assignments on time.

Absences: For absences from class, it is still the student's responsibility to turn in assignments due that day prior to class time in order to receive credit. In addition, students should obtain a copy of the work done in class from a classmate in order to stay caught up in the course. In the case of an excused absence (e.g. DSS accommodations, illness, unsafe commute due to weather safety recommendations, military duty, jury duty, official UAB activities), the student must inform the instructor prior to their absence and must send the instructor a copy of the missed classwork via email from the day of their absence in order to receive participation credit that day, after discussing with a classmate what was missed that day. Note: Students with an unexcused absence are still expected to stay caught up with work but do not receive participation credit for their absence.

If a student has an unplanned or emergency circumstance that temporarily prevents them from participating in the class for an extended period of time (e.g. documented hospitalization, mandated isolation for COVID-19, jury duty), then the instructor should be contacted to discuss.

Inclement Weather:

Class will be canceled for weather <u>only</u> if UAB cancels classes as communicated through the university's official emergency notification system. Otherwise, class will be held as scheduled.

Instructor Support - Emails & Office Hours:

I will respond to your emails as promptly as possible (usually within 24 hours, except on weekends). If you email me after 5pm, expect a response the next day unless it is over the weekend in which case I will respond the beginning of the following week. Please check your email and Canvas course regularly for announcements and updated class documents. Students are expected to check their UAB email daily and respond within 24 hours to instructor emails (with the exception of weekends). All students are required to obtain and use the UAB email address that is automatically assigned to them as UAB students, as official correspondence will be sent ONLY to your @UAB.edu email address.

During office hours, you may drop by without making an appointment to receive assistance on any assignment.

AI Tools:

The use of AI tools is strictly prohibited in this course unless otherwise announced. Academic misconduct is present in an academic work wherever AI assistance has been used when unauthorized. Such behavior is considered deceit and a violation of UAB's shared commitment to truth and academic integrity. Deceit constitutes academic misconduct and is subject to review according to UAB's Academic Integrity Code. The developments around AI are in flux and the rules that are expressed in this syllabus are subject to change on short notice.

Success Tips:

Hard work goes a long way and the more effort you put in, the more understanding you will have – that includes coming to class on time, fully participating in the activities of the day, and spending 6-8 hours outside of class completing assignments, reviewing notes, and reading for understanding. Actively participating in class dialogue, rather than simply observing, is essential for understanding. Most importantly, ask questions – inside the classroom, in office hours, or over email. The earlier on you ask questions, the better, since concepts in mathematics build upon each other. Although you are responsible for your own learning, I encourage you to communicate with me so I know best how to help you succeed. I offer the following pieces of advice for your consideration:

- Review notes and do math every day.
- Actively participate in class every day.
- Help each other.
- Go to office hours.

- Analyze and understand your mistakes.
- Ask plenty of questions.
- Don't let yourself get behind.
- Go to the Math Learning Lab.

UAB Policies & Resources:

Math Learning Lab (MLL):

Located in Heritage Hall 202, the MLL offers in-person tutoring (no appointment needed, open

Monday through Friday from first to last day of classes except holidays, breaks, and Final Exam week). No food or drink is allowed except bottled water.

University Academic Success Center (UASC):

The UASC provides students with a host of free services and resources that include Tutoring and Supplemental Instruction. For more information, click here.

Academic Misconduct:

UAB expects all members of its academic community to function according to the highest ethical and professional standards. This is outlined in the University's Academic Integrity Code found here.

Disability Support Services (DSS) Accessibility Statement:

UAB is committed to providing an accessible learning experience for all students. If you are a student with a disability that qualifies under the Americans with Disabilities Act (ADA) and/or Section 504 of the Rehabilitation Act, and you require accommodations, please contact Disability Support Services (call 205-934-4205, visit their website, or visit their office located in Hill Student Center Suite 409) for information on accommodations, registration, and procedures. Requests for reasonable accommodations involve an interactive process and consist of a collaborative effort among the student, DSS, faculty, and staff. If you are already registered with DSS, please contact them to discuss accommodations that may be necessary in this course.

Title IX Statement:

In accordance with Title IX, UAB does not discriminate on the basis of gender in any of its programs or services. The University is committed to providing an environment free from discrimination based on gender and expects individuals who live, work, teach, and study within this community to contribute positively to the environment and to refrain from behaviors that threaten the freedom or respect that every member of our community deserves. For more information about Title IX, policy, reporting, protections, resources, and supports, please visit the UAB Title IX webpage.

Student Counseling Services:

Student Counseling Services supports students in achieving personal, academic, and lifelong goals by providing individual and group mental health services, prevention and outreach programming, crisis and emergency support, and consultation services. Student Counseling Services advocates for safe and inclusive learning environments in the university community. Counseling is free and confidential. You can make an appointment by calling the Student Health and Wellness Center at 205-934-5816. Their office is open Monday-Friday, 8am-5pm and is located at 1714 9th Avenue South.

Divisive Concepts:

All University faculty, instructors and teaching staff have the academic freedom to explore, discuss, and provide instruction on a wide range of topics in an academic setting. This class may present difficult, objectionable, or controversial topics for consideration, but will do so through an objective, scholarly lens designed to encourage critical thinking. Though students may be asked to share their personal views in the academic setting, no student will ever be required to assent or agree with any concept considered "divisive" under Alabama law, nor penalized for refusing to support or endorse such a concept. All students are strongly encouraged to think independently and analytically about all material presented in class and may express

their views in a time, place, and manner, consistent with class organization and structure, and in accordance with the University's commitment to free and open thought, inquiry, and expressions.

Shared Values Statement:

Collaboration, integrity, respect, and excellence are core values of our institution and affirm what it means to be a UAB community member. A key foundation of UAB is diversity. At UAB, everybody counts every day. UAB is committed to fostering a respectful, accessible and open campus environment. We value every member of our campus and the richly different perspectives, characteristics and life experiences that contribute to UAB's unique environment. UAB values and cultivates access, engagement and opportunity in our research, learning, clinical, and work environments. Our university aims to create an open and welcoming environment and to support the success of all UAB community members.

Tentative Schedule

Class #	Date	In-Class	Assignment Due
1	W: Jan 15	Course Intro	
		Navigating the Pentagon Intro	
		Group Task: Tile Stacks	
		Group Task: Flowerbeds	
		Group Task: Function Families	
		Pre-Assessment	
-	T: Jan 21		Last Day to Drop/Add
2	W: Jan 22	Group Task: Function Families (cont'd)	
		Number Talk Intro	
		Group Task: Navigating the Pentagon	
		Group Task: Expressions make sense?	
		Menu 1 handed out	
		Menu 1 work: Growing Dots A,B,C	
3	W: Jan 29	Number Talk	Reading Reflection #1
		Discuss: Ruth Parker article	
		Group Task: Card Set A,B,C	
		Group Task: One pattern: Three Expressions Task	
		Group Task: Roller Coaster Task	
		Menu 1 work: Dalia's Graphs	
4	W: Feb 5	Number Talk	Reading Reflection #2
		Discuss: Skemp article	
		Group Task: Squareable Numbers	
		Menu 1 work: So What's Next?	
5	W: Feb 12	Number Talk	Menu 1
		Group Task: Always, Sometimes, Never True?	
		Group Task: Café Allegro Task	
		Menu 2 handed out	
		Menu 2: In/Out Tables	
6	W: Feb 19	Menu 1 Feedback & Share Ways of Seeing	Reading Reflection #3
		Student Number Talk #1	
		Discuss: Reinhart article	
		Group Task: Is it a function?	
		Midterm Review	
7	W: Feb 26	Midterm Exam	
8	W: Mar 5	Midterm Exam Feedback & Share Ways of Seeing	Reading Reflection #4
		Student Number Talk #2	
		Discuss: Thinking Classroom article	
		Exploding Dots: Intro	
_	Mar 10-16	Spring Break - No Classes	

Class #	Date	In-Class	Assignment Due
9	W: Mar 19	Student Number Talk #3	
		Exploding Dots: Insight	
		Seeing Red Task	
		Project handed out	
10	W: Mar 26	Student Number Talk #4	Reading Reflection #5
		Discuss: Knuth article	
		Car Crash Task	
		Exploding Dots: Addition	
_	F: Mar 28		Last Day to Withdraw ("W")
11	W: Apr 2	Student Number Talk #5	Menu 2
		Group Task: Averages	
		Exploding Dots: Multiplication	
		Group Task: Suzzy's Way of Multiplication	
		Portfolio handed out	
12	W: Apr 9	Menu 2 Feedback & Share Ways of Seeing	Reading Reflection #6
		Student Number Talk #6	
		Discuss: Su article	
		Group Task: Base 8	
		Group Task: Multiplication Tables	
		Exploding Dots: Subtraction	
13	W: Apr 16	Student Number Talk #7	Project
		Group Task: Base 8 Arithmetic	
		Exploding Dots: Division	
		Share Projects	
		Pre- and Post-Assessments handed out	
14	W: Apr 23	IDEA Surveys	Portfolio
		Student Number Talk #8	
		Exploding Dots: Place Value & All Bases	
		Exploding Dots: Infinite Sums	
		Take-Home Final Exam handed out	
	W: Apr 30		Take-Home Final by 7pm

Note: The course syllabus and schedule serve as a contract by which the student must comply. The syllabus and schedule are subject to changes through announcements made in class and/or email.