## TEST 2

Duration 75 min, Max. Points: 45

Make sure to show all your work and <u>underline</u> your final results. Write on these sheets or use extra paper if needed. Each subproblem is worth 3 points. Good luck!

1. Determine whether the given improper integral is convergent or divergent. To this end you may or may not need to evaluate it.

(a) 
$$\int_{-7}^{\infty} \frac{1}{e^x} dx$$

$$(b) \quad \int_1^\infty \frac{(\sin x)^2}{x^2 \sqrt{x} + 3} \, dx$$

$$(c) \quad \int_2^\infty \frac{1}{\sqrt{x^2 - 1}} \, dx.$$

**2.** Is the given SEQUENCE convergent or divergent? Justify your answer! If it is convergent find the limit.

(a) 
$$a_n = \frac{1 - 7n + n^2}{3n^2 - 8n}$$

$$(b) \quad a_n = \frac{4^n}{3^{n+5}}$$

$$(c) \quad a_n = \frac{\ln n}{n^{2/3}}$$

(d) 
$$a_n = (-1)^n \frac{n+2}{n^{-1/2} + 3n}$$

**3.** Express the number as a ratio of integers.

7.1363636...

4. Find the sum of the series

$$1 - \frac{1}{4} + \frac{1}{9} - \frac{1}{16} + \frac{1}{25} - \dots$$

with an accuracy of 0.02.

5. Determine whether the given SERIES is convergent or divergent. Justify your answer! You don't need to find the sum.

$$(a) \quad \sum_{n=1}^{\infty} \frac{2n+3}{n+\sqrt{n}-1}$$

$$(b) \quad \sum_{n=1}^{\infty} ne^{-n}$$

(c) 
$$\sum_{n=1}^{\infty} (-1)^n \sin(1/n)$$

$$(d) \quad \sum_{n=1}^{\infty} \frac{n^2}{3^n}$$

$$(e) \quad \sum_{n=1}^{\infty} \frac{\sqrt{n} - 1}{n^2 + n}$$

6. Sketch the region bounded by the curves

$$y = x^2$$
,  $y = 0$ ,  $x = 0$ ,  $x = 2$ ,

and compute the volume of the solid obtained by rotating this region about the x-axis.